

isolate the component of the stator current, thus producing a flux.

The q -axis component of the stator reference current, i_{qs}^* , may be computed using the reference input torque (T_e^*) as:

$$i_{qs}^* = \frac{2}{3} \cdot \frac{2}{p} \cdot \frac{L_r}{L_m} \cdot \frac{T_e^*}{|\psi_r|_{est}} \quad (1)$$

where $|\psi_r|_{est}$ the estimated flux of the rotor, is given by:

$$|\psi_r|_{est} = \frac{L_m i_{ds}}{1 + \tau_r s} \quad (2)$$

with L_m and τ_r are the magnetization inductance, rotor time constant, respectively.

The d -axis component of the stator reference current, i_{ds}^* , also may be obtained by using the reference input flux ($|\psi_r|_{est}^*$) as:

$$i_{ds}^* = \frac{|\psi_r|_{est}^*}{L_m} \quad (3)$$

By using the rotor speed, ω_m , and the slip frequency given by equation (4):

$$\omega_{s1} = \frac{L_m}{|\psi_r|_{est}} \cdot \frac{R_r}{L_r} \cdot i_{qs}^* \quad (4)$$

The angle of the rotor flux may be evaluated using the equation (5):

$$\theta_e = \int (\omega_m + \omega_{s1}) dt \quad (5)$$

where R_r and L_r are the rotor resistance and inductance respectively.

The reference currents of the stator i_{ds}^* and i_{qs}^* after transferring to phase currents (i_a^* , i_b^* and i_c^*) are entered to current regulators section. The current regulators section produces the patterns of the switches of the inverter (S_a , S_b and S_c).

B. Direct Torque Control

In addition to vector control systems, instantaneous torque control yielding fast torque response may also be obtained by employing DTC method. The DTC was developed more than a decade ago by Japanese and German researchers (Takahashi and Noguchi 1984, 1985; Depenborck 1985) [5]. The basic idea in the DTC control, which block diagram shown in Fig. 2, is to choose the optimal vector voltage, for which the generated rotated flux produces the desired torque [4]. The DTC technique is based on the theory of the FOC induction motor and direct self control method. The core of the DTC consists of hysteresis controllers of the torque and flux; optimal switching logic; precise motor model.

The space vector of the stator flux ($\bar{\psi}_s$) is calculated by using:

$$\bar{\psi}_s = \int (\bar{V}_s - R_s \bar{I}_s) dt \quad (6)$$

With the vector quantities stator voltage (\bar{V}_s) and current \bar{I}_s are being obtained using equations (7) and (8) respectively.

$$\bar{V}_s = \frac{2V_{dc}}{3} \left[S_a + S_b e^{j\frac{2\pi}{3}} + S_c e^{j\frac{4\pi}{3}} \right] \quad (7)$$

$$\bar{I}_s = \frac{2}{3} \left[i_a + i_b e^{j\frac{2\pi}{3}} + i_c e^{j\frac{4\pi}{3}} \right] \quad (8)$$

where V_{dc} , S_i and i_k ($i, k = a, b, c$) are DC voltage, the signals of the gates of the inverter and the stator measured currents, respectively.

Finally, the electromagnetic torque T_e may be calculated using:

$$T_e = \frac{3P}{2} (\bar{I}_s \cdot j\bar{\psi}_s) \quad (9)$$

The motor model calculates the torque, stator flux and shaft speed based on the measurements of two-phase current and the circuit dc voltage. Torque and flux references are compared with these values, and control signals are produced using a two level hysteresis. The optimal switching logic defines the best vector voltage based on the torque and flux references [6].

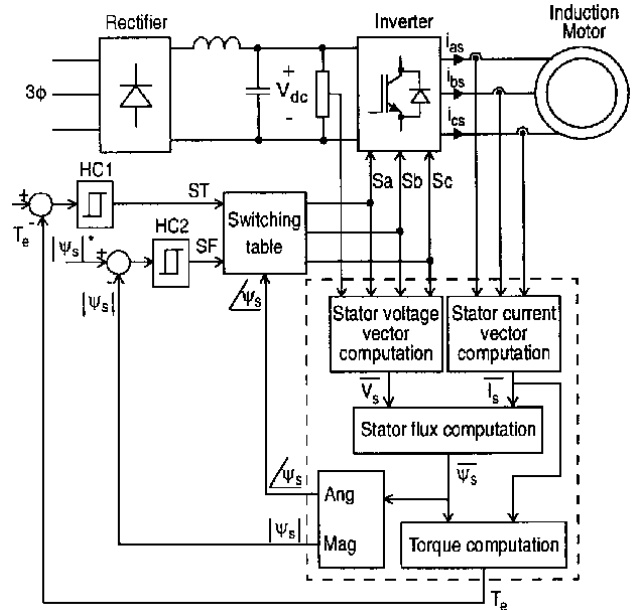


Fig 2: Block diagram of the DTC technique

III. THE SIMULATION RESULTS

Simulations of the FOC and DTC techniques have been performed for a 50^{PH} induction motor, with data being listed in the appendix. In each case, a three-phase inverter feeds the induction motor. The frequency switching for both cases are different, and depend on hysteresis controllers. However, the parameters are chosen as such that the frequency range is the same.

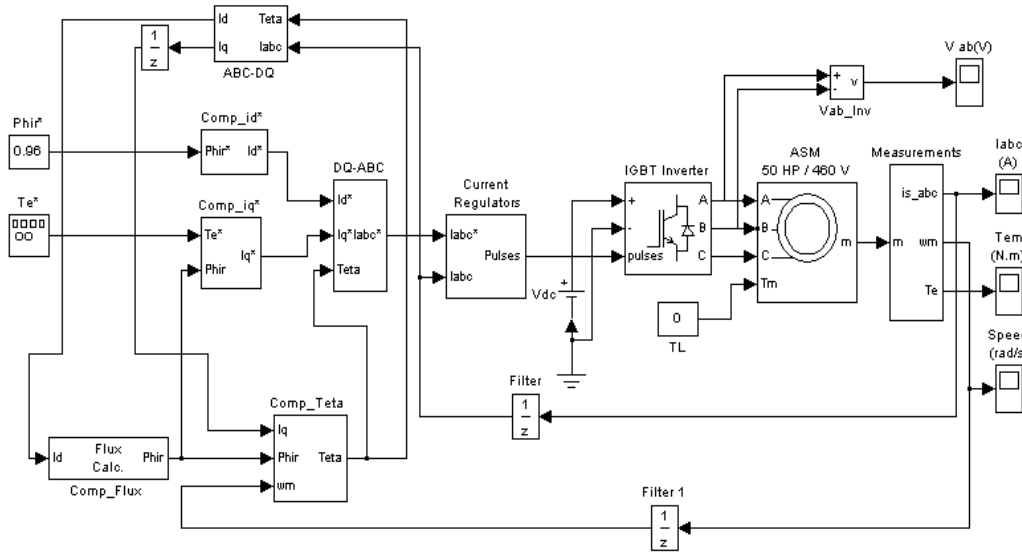


Fig. 3: The simulink model for FOC technique

Using FOC technique, the band of the hysteresis current controller is 10^A , and using DTC, the bands of the hysteresis flux and torque controllers are 0.2^{Wb} and $40^{N.m}$, respectively.

To investigate the dynamic operation of the torque, a square wave with amplitude $200^{N.m}$ is applied to the torque while the reference of the flux being fixed at rating value. The motor operates with low speed, and the switching time is approximately 0.5^{ms} .

To investigate the operation of the flux, we decrease the input control flux to be 0.75 percent of the rating value, while keeping of the torque fixed.

Next, we first describe the simulation for both of methods and then provide the simulation results.

A. The FOC method

Fig. 3 shows the simulink model of the FOC technique, where the q -axis component of the stator current is being considered. Therefore, the operation of the control system depends on the stator currents regulators. Due to the fast response, the hysteresis controllers are used. Therefore, the switching frequency of the inverter will be variable and will depend on the operation conditions. The variation of the torque is proportional to the variation of the q -axis component of the stator current:

$$\frac{\Delta T_e}{\Delta t} = \frac{3}{2} \cdot \frac{P}{2} \cdot \frac{L_m}{L_r} \cdot |\psi_r| \cdot \frac{\Delta i_{qs}}{\Delta t} \quad (10)$$

Figs. 4 and 5 show the simulation results for the FOC technique.

At FOC technique, as the Fig. 5 shows the stator and rotor flux's change with the time constant equal to the rotor time constant (in this case $\tau_r=0.156^S$).

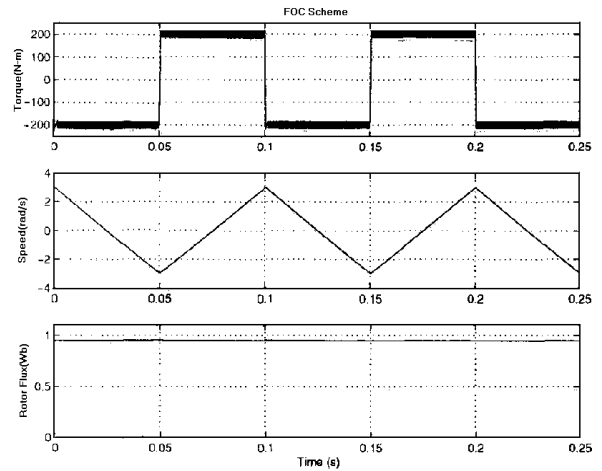


Fig. 4: The step response of the torque control in FOC technique

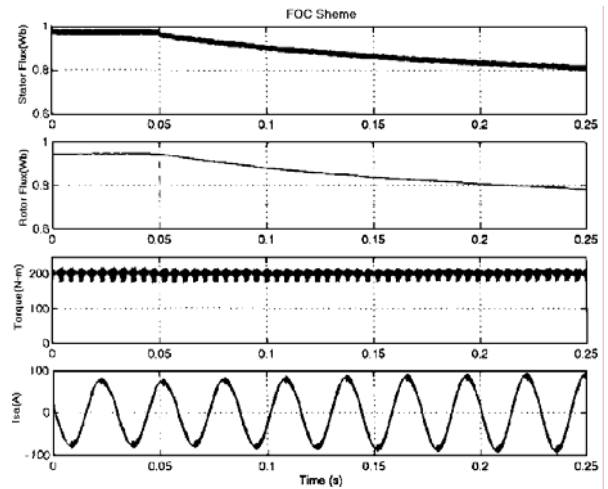


Fig. 5: The step response of the flux control in FOC technique

However, a direct torque controlled motor suffers from great torque ripple due to the fast response of the torque. The most important characteristic of DTC is its fast torque response. When a proper vector is applied to motor, the stator flux vector rotates very fast and the angle between the stator flux and rotor flux is increased [4]. Direct torque control (DTC) is used to control the motor. In this control strategy, efficiency is optimized by adjusting the magnetic flux of the motor [6].

The important characteristics of the DTC method are:

- Direct control of stator flux and electromagnetic torque and indirect control of stator currents and voltages;
- Almost sinusoidal stator fluxes and currents;
- Reduced torque oscillations;
- Excellent torque dynamics;
- Inverter switching frequency depending on flux and torque hysteresis bands.

The main advantages of the DTC method are:

- Absence of coordinated transformations (which are required in most of the vector-controlled drive implementations), separate voltage modulation block (required in vector drives) and voltage decoupling circuits (required in voltage-source inverter-fed vector drives);
- Reduced number of controllers
- Determination of the actual flux-linkage vector position is not necessary only the sector where the flux linkage is located.

The main disadvantages of a conventional DTC method are:

- Starting, low-speed operation and torque changes could be of some concern.
- The flux-linkage and electromagnetic torque estimator are needed.
- Variable switching frequency [5].

IV. CONCLUSIONS

In this paper, two methods namely FOC and DTC for controlling the induction motors are considered. Implementation of the FOC method requires having a sinusoidal reference signal, while on the contrary, due to the use of stationary reference, the DTC method does not necessitates having a sinusoidal reference signal. Finally, it can be shown that the DTC algorithm provides much faster response than FOC.

Appendix: Induction motor data

Rated power	50PHP
Rated voltage	460V
Rated frequency	60Hz
Number of poles	4
Stator resistance	$R_s=0.087\Omega$

Stator inductance	$L_s=0.8\text{mH}$
Magnetization inductance	$L_m=34.7\text{mH}$
Rotor resistance	$R_r=0.228\Omega$
Rotor inductance	$L_r=0.8\text{mH}$

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