# ANALYSING AND IMPROVING THE GAIN-FREQUENCY PERFORMANCE OF BANDPASS FILTER STRUCTURED DISTRIBUTED AMPLIFIERS

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#### ABSTRACT

In this work, methods are presented to improve the gainfrequency performance of a bandpass structured distributed amplifier (BP-DA) and the basic analysis of the performance is given. It is shown that the BP-DA is a good way to shift the gain band of a DA without decreasing the bandwidth.

# **I. INTRODUCTION**

The multioctave behaviour of the distributed amplifier makes it one of the most investigated broadband circuits. A conventional DA employs two artificial transmission lines that show lowpass (LP) filter characteristic [1-4]. It is important to increase the maximum frequency of operation of a DA. BP filter structure can be used in place of LP structure for applications not requiring DC operation [1,5,6]. The application to bandpass amplifiers was considered by Perceival [1] when the idea of distributed amplification was conceived. In the literature, there are two different BP structures proposed to increase the maximum operation frequency [5,6]. The first bandpass structure is designed and implemented by Minnis [5]. But the structure has drawbacks, since characteristic impedance  $(Z_0)$  is frequency-dependent for distributed case and this makes the bandwidth of a DA with the structure lower than that of a conventional DA (CDA or LP-DA) using the same active component. On the other hand, the second bandpass (BP) structure can shift the gain-frequency band without decreasing the bandwidth [6].

In this paper, some works made on a DA with the second BP structure (BP-DA) are presented. Basic features of this circuit are identified by means of a distributed bandpass transmission line model [6]. The effects of input parasitic resistance of transistors ( $R_i$ ) on the BP-DA are taken into account (the parasitic resistance causes frequency behaviour to deteriorate). The basic analysis is made and formulas of the gain and upper limit of the frequency behaviour can be improved by means of additional damping resistances of shunt inductances in

the gate line and lowpass T sections inserted into the artificial lines. Basic design of a DA with the BP structure can be easily made by means of the formulas and methods given in this work.

Simulations have been made on DAs which consist of four transistors. The same active component has been used for all the simulations to obtain comparable results. In the first simulation, the performances of the two different BP structure are compared. The second, by means of which we can examine the formulas given in this paper, gives us the opportunity of observing how the damping resistances change the performance of a DA with the proposed BP structure. The last illustrates the effect of the T sections inserted into the artificial lines of the BP-DA.





# **II. BASIC FORMULAS IN DISTRIBUTED CASE**

In distributed amplifiers, there are two artificial transmission lines [1-4]. These artificial lines are constructed by input and output capacitances (C) of active components and inductances (L) added to DA. The bandwidth (cut-off frequency) of a conventional DA is

$$f_{\rm c} = 1/\pi \sqrt{\rm LC} \tag{1}$$

The schematic diagram of a conventional DA is given in Figure 1. To obtain basic points of a conventional DA, formulas of transmission line which shows distributed LP structure are used [7]. As done for LP-DA, a distributed BP transmission line model can be used to obtain basic points of the BP-DA.



Figure.2 A distributed bandpass transmission line section

The model of the distributed BP transmission line section is shown in Figure 2. By using the model, the characteristic impedance ( $Z_0$ ) and propagation constant ( $\gamma$ ) formulas of the BP line can be easily obtained, as made in transmission line analysis [7]. After the routine analysis, it can be observed that  $Z_0$  is constant under the condition of

$$L_1 C_1 = L_2 C_2 \tag{2}$$

and for this case, we obtain the equations of

$$Z_{o} = \sqrt{\frac{L_{i}}{C_{2}}} = \sqrt{\frac{L_{2}}{C_{i}}}$$
(3)

$$\gamma = j \frac{\omega^2 L_2 C_2 - l}{\omega} \frac{l}{\sqrt{L_2 C_1}}$$
(4)

From Eqs. (4) and (2), it can be easily observed that  $\gamma=0$  for

$$\omega_0 = \sqrt{\frac{1}{L_2 C_2}} = \sqrt{\frac{1}{L_1 C_1}} \tag{5}$$

As explained above, two different BP structure have been presented in the literature. Figure 2 shows the second BP structure [6]. In the previously used BP structure [5], a shunt inductance ( $L_2$ ) is used in addition to the lowpass case and  $C_1$  is not used. In that case, Eq. (3) changes to

$$Z_{\theta} = \sqrt{\frac{Z}{Y}} = \sqrt{\frac{sL_1}{\frac{l}{sL_2} + sC_2}}$$
(6)

It is easily seen from this equation that  $Z_0$  does not remain constant with frequency and approaches  $\sqrt{L_1/C_2}$  as frequency increases. Therefore, the gainfrequency performance of a DA with the structure is poor at low frequencies. As a result, bandwidth of a DA with the previously used BP structure is narrower than that of a LP-DA (CDA) using the same active component.

## III. BASIC ANALYSIS AND DESIGN OF THE BPDA

As in the lowpass case, while changing the distributed BP structure used in this work into lumped BP structure, we see that Eq. (3) and Eq. (4) can be used for  $Z_0$  and  $\gamma$  in a limited band whose geometric center frequency is  $\omega_0$  given in Eq (5).



Figure.3 A DA with the bandpass filter structure

The schematic diagram of the BP-DA is given in Figure 3. It can be seen from passive filter transformations [8] that the BP structure, as in the LP case, has a bandwidth of

$$BW = 1/\pi \sqrt{L_1 C_2} \tag{7}$$

If  $\omega_{\!L}$  is the lower limit and  $\omega_{\!U}$  is the upper limit of the band, then

$$\omega_0 = \sqrt{\omega_L \omega_U} \tag{8}$$

On the other hand, Eq. (2) can be shown as

$$\frac{C_1}{C_2} = \frac{L_2}{L_1} = k \tag{9}$$

Using Eqs. (5), (7)-(9), we obtain that the upper limit of the band is

$$f_{U} = \frac{I + \sqrt{I + \frac{I}{k}}}{2} \frac{I}{\pi \sqrt{L_{1}C_{2}}} = b f_{c}$$
(10)

As known,  $f_C$  given in Eq. (1) is the cutoff frequency of a LP-DA. Therefore, b is the ratio of the upper limits of the BP-DA and LP-DA. On the other hand, if the aimed ratio of the upper limits of the DAs is b, then

$$k = \frac{C_1}{C_2} = \frac{L_2}{L_1} = \frac{l}{4(b^2 - b)}$$
(11)

can be used to obtain values of  $C_1$  and  $L_2$ .



One of the important problems in a DA is the input parasitic resistance  $R_i$  of the transistors. The simplified model of a FET including  $R_i$  is illustrated in Figure 4.  $R_i$ causes a shunt conductance at the input of the active component, which increases rapidly with frequency. The shunt conductance in the gate-line can be approximated as

$$G_{i} \cong \omega^{2} C_{gs}^{2} R_{i}$$
<sup>(12)</sup>

for each transistor [4]. Therefore, the upper frequency limit of a conventional DA is always lower than the cutoff frequency ( $f_c$ ) of the artificial line [3].

It is clear that the gate-line loading also exists in a DA with BP filter structure [6]. Therefore, a big peaking at the lower limit of the frequency band occurs in BP-DA; the input resistance  $R_i$  causes the gain to decrease in the upper region of the band. On the other hand, there are not damping resistances of the shunt inductances, which cause gain to decrease in the lower region of the frequency band. Therefore, the damping resistances ( $R_b$ ) can be used to suppress the peaking. In case of  $R_b \cong R_i$ , the effect of  $R_b$  on the gain in the lower region is almost the same as that of  $R_i$  in the upper region.



Gate-line of the improved BP-DA is shown in Figure 5. Like  $R_i$ , the damping resistance causes a shunt conductance in the gate-line. As a result, the shunt conductance is approximately obtained as

$$G_2 \cong \frac{R_b}{\omega^2 L_b^2} \tag{13}$$

As explained above, the phase shift per BP section is zero at the center frequency. If the number of transistors is n, then the total conductance's in the gate and drain lines at the center frequency will be, respectively,

$$G_{gT} = \frac{l}{R_{-}} \cong \frac{n(R_i + R_b)}{Z_i^2 k}$$
(14)

$$G_{dT} = \frac{l}{R_{dT}} = \frac{n}{R_{ds}}$$
(15)

We can easily obtain the voltage gain from the source to the gate-line using Eq. (14) and the voltage gain from the gate-line to the load using Eq (15);

$$A_{I} \cong \frac{Z_{Ig} / / R_{gT}}{Z_{Ig} / / R_{gT} + Z_{g}}$$
(16a)

$$A_2 \cong -ng_m \left( R_{dT} //Z_{td} //Z_L \right)$$
(16b)

In Eq. (16a)  $Z_{tg}$  is the termination resistance of the gateline and  $Z_g$  is the source resistance. In Eq (16b)  $Z_{td}$  is the termination resistance of the drain-line and  $Z_L$  is the load resistance. If  $Z_g=Z_L$  and both are real, it can be easily shown that  $S_{21}$  of the BP-DA is



Figure.6 A lowpass T section

As mentioned above, the phase shift per BP section is zero at the center frequency. In that case, the shunt conductances at the input and output of the transistors appear in parallel and Eqs. (14) and (15) are obtained. Therefore R<sub>i</sub>, R<sub>b</sub> and R<sub>ds</sub> cause the gain of the BP-DA to decrease and to show a minimum at the center frequency (this gain can be calculated by using Eqs. (16) and (17)). The decrease in the gain can be reduced if the phase differences between signals of neighbouring transistors are made non-zero at the center frequency. Inserting lowpass T sections into the artificial BP lines, we can achieve this, since an LP-T section has a non-zero phase difference for non-zero frequencies. In this way, the summing of the shunt conductances can be avoided. This helps the gain to increase at the center frequency. Figure 6 shows an LP-T section [4]. The characteristic impedance of the T section should be the same as that of the artificial lines, i.e.

$$\sqrt{\frac{L_e}{C_e}} = Z_0 \tag{18}$$

and its cut-off frequency should be equal to or higher than the upper frequency limit of the BP-DA, i.e.

$$\frac{1}{\pi \sqrt{L_e C_e}} \ge f_u \tag{19}$$

The characteristic impedance change of the LP-T section versus frequency is not the same as that of the BP section. This may be cause the performance of the BP-DA to deteriorate. Therefore, we must decide on the number of T sections to be used and where to insert these sections. Our investigations show that using two lowpass T sections and inserting them between the transistors in the middle give the best performance improvement. Figure 7 below shows the schematic diagram of the proposed BP-DA.



Figure.7 The proposed BP-DA with extra LP-T sections and damping resistances R<sub>b</sub>



Figure.8 The gain-frequency characteristics of the BP structures



Figure.9 Gain-frequency characteristics of the BP-DA improved by  $R_{\rm b}$  and LP-DA



Figure.10 Frequency response of the proposed BP-DA

#### **IV. SIMULATION RESULTS AND DISCUSSION**

The small signal FET model used in simulations is illustrated in Figure 4. The DAs used in the simulations consist of four transistors. Element values of the model been extracted from measurements of a have commercially available 300-µm GaAs MESFET. The values are Cgs=0.35pF, Cds=0.14pf, Ri=6Ω, Rds=1500Ω and gm=70mS. As seen,  $C_{ds}$  is smaller than  $C_{gs}$ . In practice, the characteristic impedances and the delays of the input and output lines are aimed to be equal. Therefore, an extra capacitance is used to satisfy  $C_{ds}=C_{gs}$ . Figure 8 shows the gain-frequency characteristics of the previous and proposed BP structures. For this simulation, element values are L=0.875nH, Cb=0.42F ve Lb=1.05nH. and  $C_b/C_{gs}=L_b/L=1.2$  has been chosen. It is clear that L must be 0.875nH for  $Z_0 = \sqrt{L/C_{gs}} = 50\Omega$ . As can be observed from Figure 8, the bandwidth of the DA with the previously used BP structure is lower than that of the DA with the BP structure used in this work.

It can be observed from Figure 8 that there is a large peaking at the lower limit of the frequency band of the DA with the proposed BP structure. As mentioned above, the peaking can be suppressed by means of damping resistances of the shunt inductors in the gate line. Figure 9 shows the gain frequency characteristics of the BP-DA with  $6\Omega$  damping resistances and the LP-DA. It is clear from Figure 9 that the damping resistances improve the gain-frequency characteristic. The gain of the BP-DA is ~11dB which is ~2dB lower than that of the LP-DA. It can be observed from the figure that the bandwidth of the BP-DA is ~14.5GHz. This is approximately equal to that of the LP-DA (~15GHz). Figure 9 is also convenient for examining the formulas given for the upper frequency limit and the gain at the center frequency. k=1.2 has been chosen for the BP-DA. Then b is approximately calculated as 1.177. The simulation results give the upper frequency limit of the LP-DA as 14.95GHz and that of the BP-DA as 18.25GHz. Thus,  $b \cong 1.22$  is obtained at the end of the simulations. The reason of the difference is that Eq.(10) has been obtained for R<sub>i</sub>=0 and simulations have been carried out for  $R_i=6$ . On the other hand, using Eqs.(16) and (17) given for gain, we calculate  $|S_{21}|$  as 9.63 dB at the center frequency ( $\omega_0$ =8.3GHz). As a result, the calculated value is approximately equal to the value obtained by the simulation and the average value of  $|S_{21}|$  is approximately 1 dB higher.

It is clear from Figure 9 that the gain of the BP-DA decreases at the center frequency. To reduce the decrease in the gain, two lowpass T sections have been used. The proposed BP-DA is illustrated in Figure 7.  $R_b=5.25\Omega$  has been chosen to obtain the best performance. The T sections have been inserted between the second and third transistors. The gain-frequency characteristic of the proposed BP-DA is illustrated in Figure 10. The T sections have caused ripples in the frequency band because the characteristic impedance change of the T

section versus frequency is not the same as that of the BP sections. The maximum ripple in the gain-frequency characteristic of the proposed BP-DA is 1.26dB. The ripple in the gain-frequency characteristic of the BP-DA without the T sections is 2 dB. Thus, the maximum ripple has been reduced by ~0.75dB. It can be seen from Figure 9 and 10 that the average value of  $|S_{21}|$  and the bandwidth have not changed.

Another important point for a DA is phase response. The phase response of the BP-DA is approximately linear within the pass-band. But, the linearity deteriorates in the lower region of the band. The reason is that the BP structure shows highpass behaviour in this region (One can see the same point by investigating Eq (4) given for  $\gamma$ ). It may be useful to take this point into account for applications of the BP-DA.

# V. CONCLUSION

In this work, a DA with BP filter structure is presented to shift the frequency band of operation of a distributed amplifier and analysed by means of a distributed bandpass transmission line model. The basic analysis has been made and formulas of the gain and upper frequency limit have been given. Then, methods have been introduced in order to improve the gain-frequency behaviour. The basic design of a DA with the BP structure can be made by means of the formulas and methods given in this paper. Consequently, it has been shown that, despite the lower gain, the BP-DA improved by the methods is a good way to increase the maximum frequency of operation of a DA for applications not requiring DC operation.

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